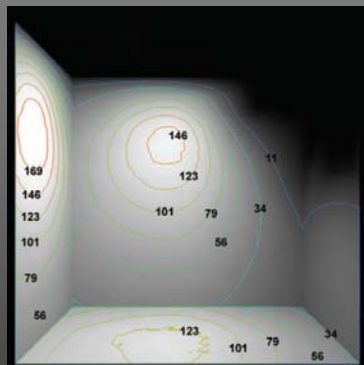


## Lighting Math

### NOT SO SCARY LIGHTING MATH



### NOT SO SCARY LIGHTING MATH



#### The importance of Lighting Math:

- Calculations can determine the light levels
- Calculations can determine the required quantity of fixtures
- Calculations can verify layout

#### Methods to perform Lighting Math:

- By Hand
- By Computer

# Lighting Math

## Target Illuminance / Light Levels

### Who Defines Light Levels?

- IES of North America
  - Recommended Practices
  - Defines light levels and quality of illumination by task and application
- Codes and Regulations
- The Owner



*Definitions:*      **Task** = the work performed

**Applications** = the project type (i.e. School, Commercial etc,

- IESNA Light Level recommendations are for Foot-candles at the work plane (2'6" AFF)
- They have limited significance to us when we interpret the actual environment.
- Such factors as lighting walls, brightness accents, shadows, sparkle, and color have a greater influence on emotional reaction.
- IESNA's recommend light levels are for an age range of 40 – 55 years old

<i>Orientation and simple visual tasks.</i> Visual performance is largely unimportant. These tasks are found in public spaces where reading and visual inspection are only occasionally performed. Higher levels are recommended for tasks where visual performance is occasionally important.		
A	Public spaces	30 lx (3 fc)
B	Simple orientation for short visits	50 lx (5 fc)
C	Working spaces where simple visual tasks are performed	100 lx (10 fc)
<i>Common visual tasks.</i> Visual performance is important. These tasks are found in commercial, industrial and residential applications. Recommended illuminance levels differ because of the characteristics of the visual task being illuminated. Higher levels are recommended for visual tasks with critical elements of low contrast or small size.		
D	Performance of visual tasks of high contrast and large size	300 lx (30 fc)
E	Performance of visual tasks of high contrast and small size, or visual tasks of low contrast and large size	500 lx (50 fc)
F	Performance of visual tasks of low contrast and small size	1000 lx (100 fc)
<i>Special visual tasks.</i> Visual performance is of critical importance. These tasks are very specialized, including those with very small or very low contrast critical elements. Recommended illuminance levels should be achieved with supplementary task lighting. Higher recommended levels are often achieved by moving the light source closer to the task.		
G	Performance of visual tasks near threshold	3000 to 10,000 lx (300 to 1000 fc)

## Lighting Math

# Ages

**Less than  
40 years  
old...**

*Can reduce  
the light  
levels up to  
1/3!*

**Standard Age Range**  
is ~~40-55~~ years old



**Over 55  
years old...**

*Can  
increase the  
light levels  
up to 2/3!*

***Babies require 3 times more light than a 20 year old!***

## IESNA Recommended Light Levels

IESNA Lighting Design Guide										Interior
I. INTERIOR LOCATIONS AND TASKS	Very Important	Important	Somewhat important		Blank = Not important or not applicable					
	<b>Design Issues</b>									
	Appearance of Space and Luminaires									
	Color Appearance (and Color Contrast)									
	Daylighting Integration and Control									
	Direct Glare									
	Flicker (and Strobe)									
	Light Distribution on Surfaces									
	Light Distribution on Task Plane (Uniformity)									
	Luminances of Room Surfaces									
	Modeling of Faces or Objects									
	Point(s) of Interest									
	Reflected Glare									
	Shadows									
	Source Task-Eye Geometry									
	Sparks/Debris Reflected Highlights									
	Surface Characteristics									
	System Control and Flexibility									
	Special Considerations									
	Notes on Special Considerations									
	Illuminance (Horizontal)									
	Category or Value (lux)									
	Illuminance (Vertical)									
	Category or Value (lux)									
	Notes on Illuminance - see end of section									
	Reference Chapter(s)									
Accounting (see Offices)										Ch 11
Air Terminals (see Transportation Terminals in Section V, Transportation)										Ch 23
Armories									C	A
Art Galleries (see Museums)										Ch 14
Auditoriums										
Assembly									C	
Social activity									B	A
Banks (see Reading)										Ch 11
Lobby										
General								(1)	C	A
Writing area								(1)	D	A
Tellers' stations								(1)	E	A

## Lighting Math

### Summary Light Level (table 15)

Activity	General Lighting			Task Lighting		
	Public Spaces	Simple Orientation	Occasional Visual Task	Large Visual Task	Small Visual Task	Very Small Visual Task
	3 fc	5 fc	10 fc	30 fc	50 fc	100 fc
<b>GENERAL</b>						
Circulation						
Corridors		*				
Elevators		*				
Lobbies			*			
Stairs		*				
Service						
Toilets and washrooms		*				
Storage						
Active			*			
Inactive		*				
<b>HOSPITALITY FACILITIES</b>						
Bathrooms, for grooming				*		
Bedrooms, for reading				*		
Cleaning			*			
Dining			*			
Kitchen, critical seeing					*	
Laundry				*		

### Measuring Light



#### Luminance

- Measures how easy something is to see, or how bright a surface is – *emitting light energy*
- Examples: backlit signage, a full moon, glowing wall
- Measured in: Foot-Lamberts (US) or Candelas per meter squared (metric)  
1 Foot-Lambert = 3.426 Candelas/m<sup>2</sup>

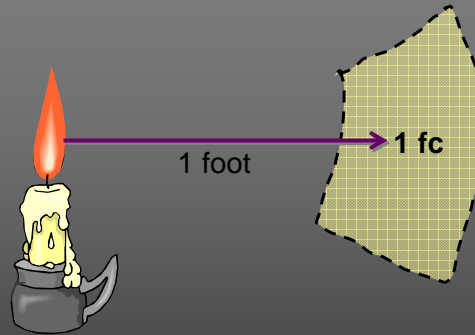


#### Illuminance

- Measures how much light there is to see by, the light level to perform a task – *arriving lighting energy*
- Examples: emergency light level on the floor,
- Measured in: Foot-Candles (US) and Lux (Metric)

## Lighting Math

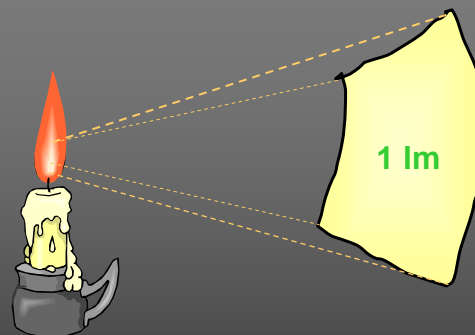
### Light – The Foot-candle



**Foot-candle** is known as a unit of light - direct illumination light level

Derived from one candle placed at a distance of one foot from a surface is defined as a **foot-candle**  
(abbreviation = fc or FC)

### Light – The Lumen



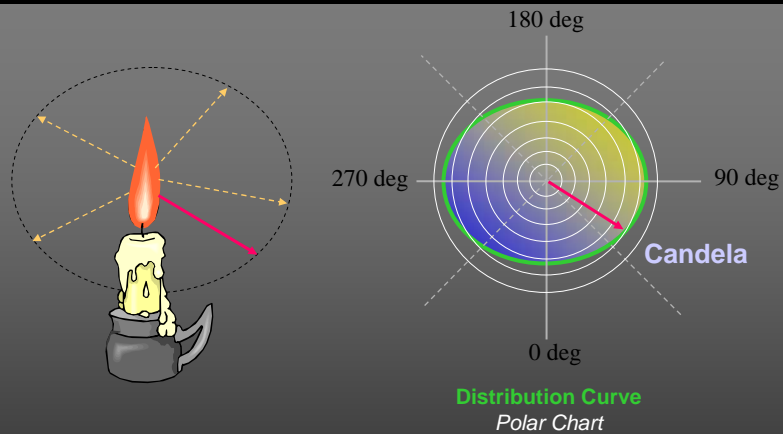
The energy of light from a candle falling on a one foot square **area** is **One Lumen** (abbreviation = lm)

*The total amount of light energy coming out of the candle is approximately 13 lumens*  
*The total amount of light energy coming out of 100-watt A-lamp is approximately 1650 lumens*

**NOT DEFINED BY DISTANCE**

## Lighting Math

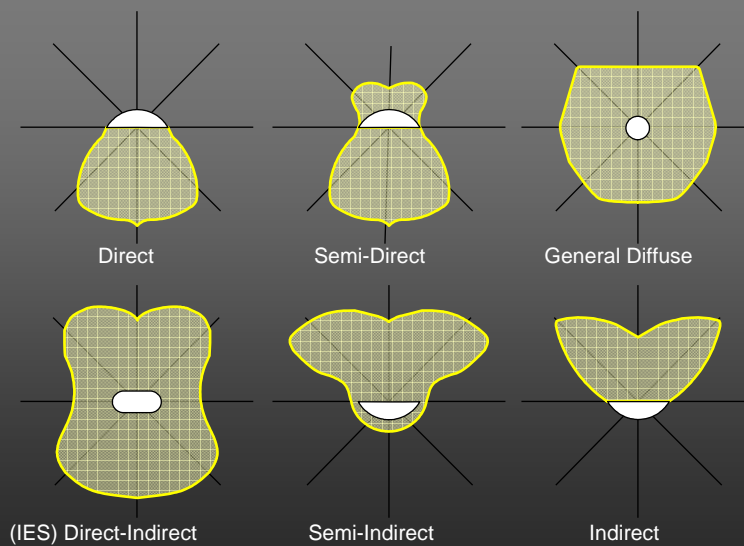
### Light – The Candela



**Candle Power** is the intensity value at any given direction.  
(unit is *Candela*, abbreviated as *cp*)

**Distribution Curve** represents the total light intensity pattern produced by a source

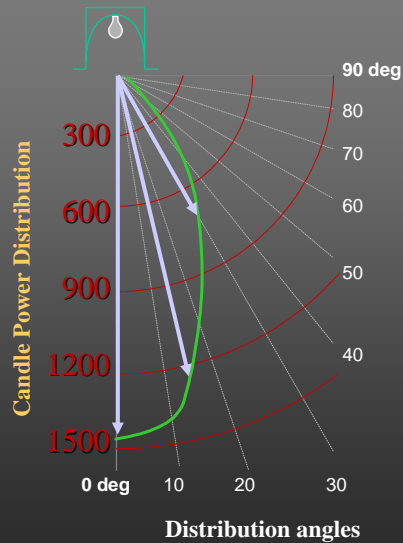
### CIE Luminaire Types / Distributions



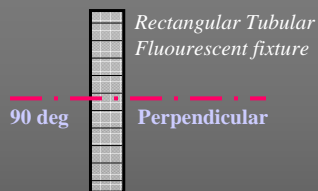
## Lighting Math

### Candlepower Distribution Curve

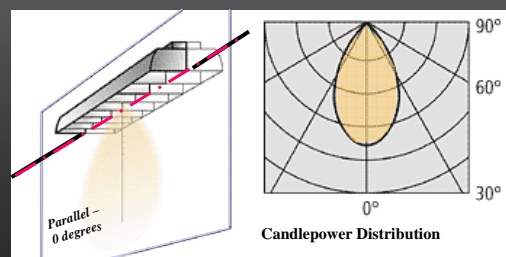
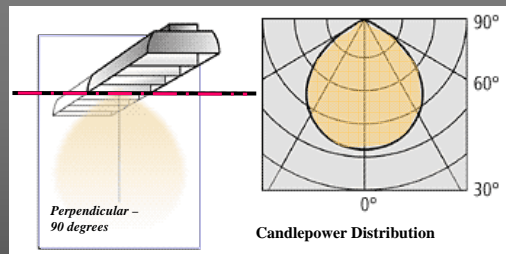
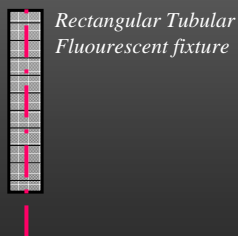
- **Candlepower distribution curves** provides intuitive information on how a **luminaire** will perform
- **Candela** values are used in calculations to predict light levels



### Asymmetrical Distribution Curve



0 deg Parallel



## Lighting Math

### Light Measurement

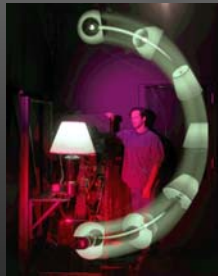
Measures the candlepower distribution of a particular lamp or luminaire.

Information is generated in a -- **Photometric report**



Erik is setting up a lamp for testing in the 2m integrating sphere.

Integrating Sphere



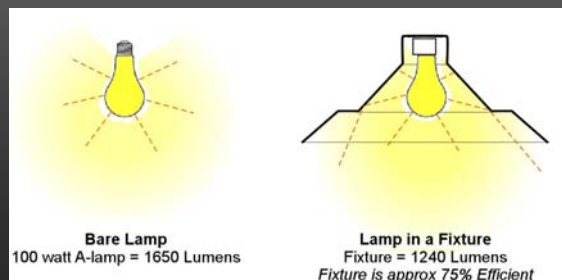
Gonio-Photometer



The Spectro-Radiometer

### Lumens versus Candelas

- **Lumen** is an amount of **ENERGY**
- **Candela** is an amount of **INTENSITY**
- Light output from lamps and fixtures be measured in **Lumens** and **Candelas**.
- Fixtures alter **Lumen** and **Candela** output (Their values can only be found in Photometry Reports)

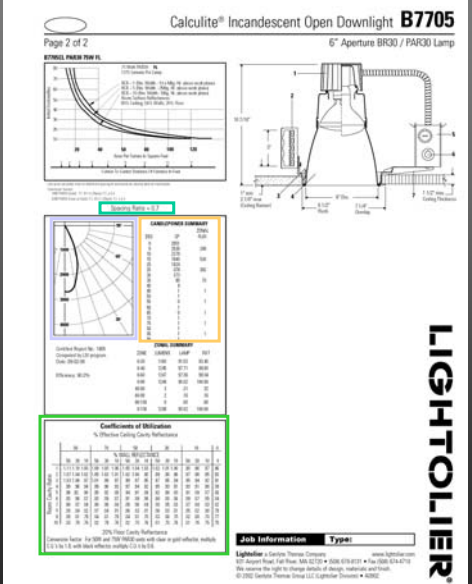




# Lighting Math

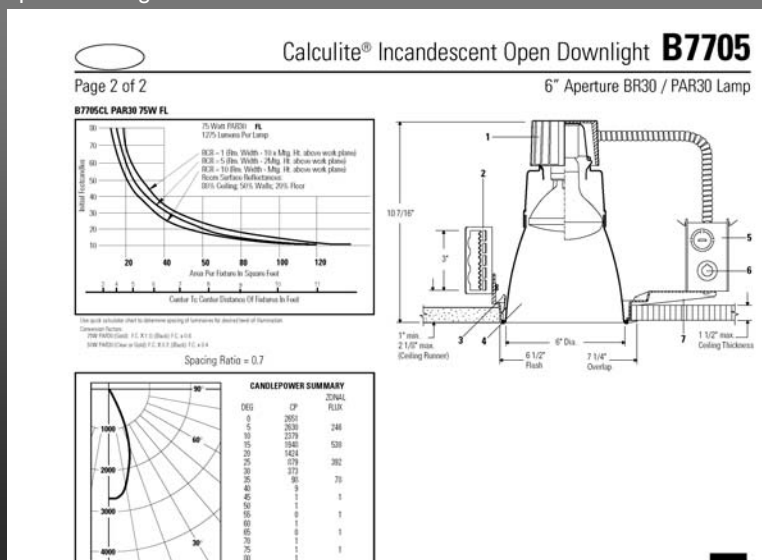
## Photometry Reports

- Plot of candlepower values
- Summary of candlepower values in different planes
- Fixture Efficiency
- Lumen Summary
- Luminance summary
- Spacing criteria (SC) or Spacing/Mounting Height (S/MH) for uniformity
- Coefficient of Utilization Table
- Guides



## Photometry Reports: sample 1

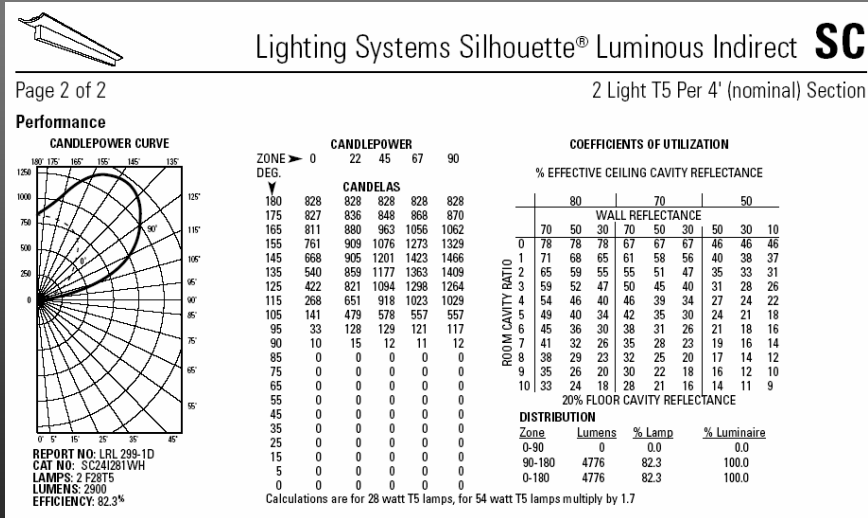
- Open Downlight



## Lighting Math

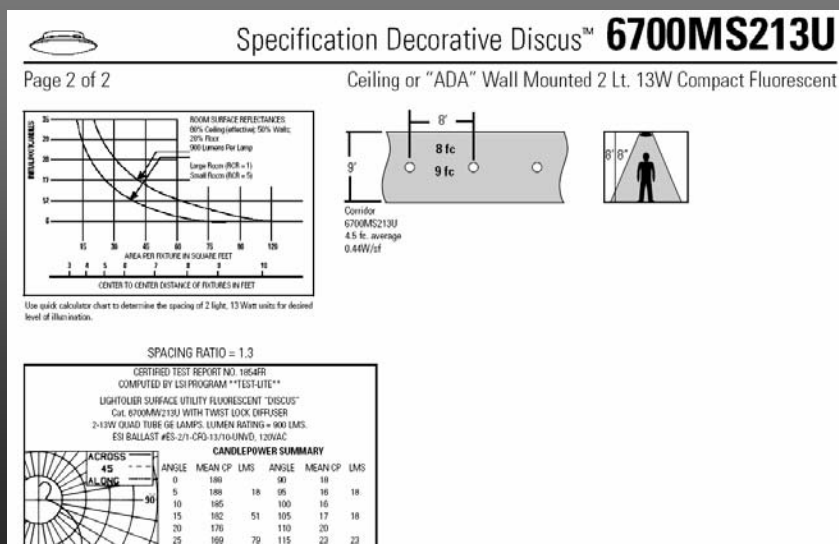
### Photometry Reports: sample 2

- Indirect Pendant



### Photometry Reports: sample 3

- Ceiling Fixture



## Lighting Math

### Hand Methods to Calculate Light

#### Mnfrs Guides

- Direct or Average Illumination from a Fixture or Lamp
- Recommended spacing or layout

#### Point-by-Point

- Direct light level from a Fixture or Lamp

#### Lumen Method

- Average Light Level in a Room from a Fixture
- Can be used to determine quantity needed

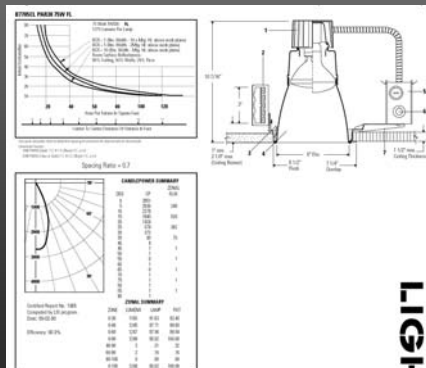
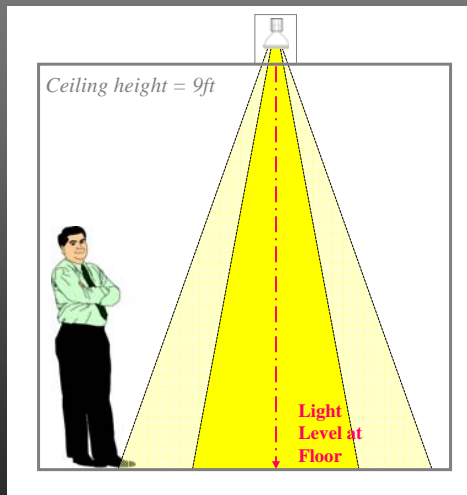
### Point-by-Point

$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

$$\text{FC} = 2651 \text{candelas} / 9\text{ft}^2$$

$$\text{FC} = 2651 / 81$$

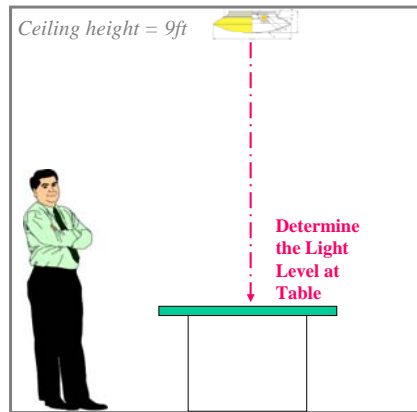
$$\text{FC} = 32.7 \text{ foot-candles}$$



## Lighting Math

# Point-by-Point

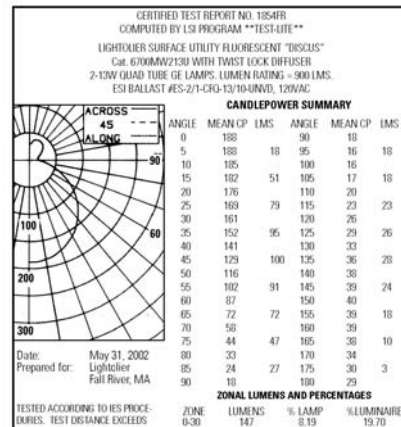
- Ceiling Fixture Example



$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

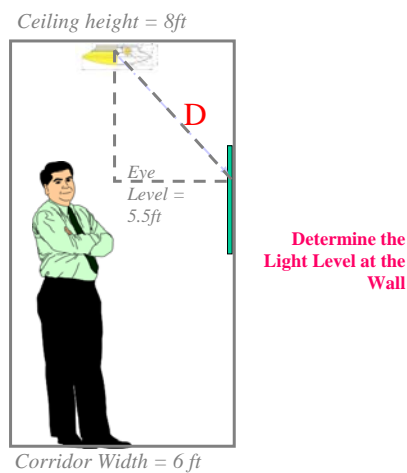
**FC** = \_\_\_\_\_ *candelas* / \_\_\_\_\_ *ft*<sup>2</sup>

**FC = \_\_\_\_\_ foot-candles**

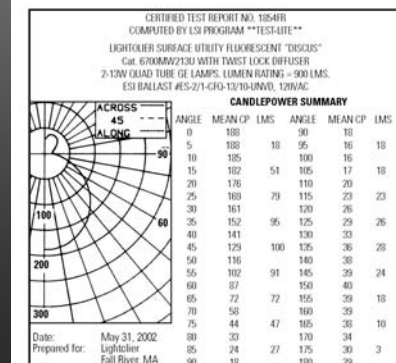


# Point-by-Point

- Ceiling Fixture Example



$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

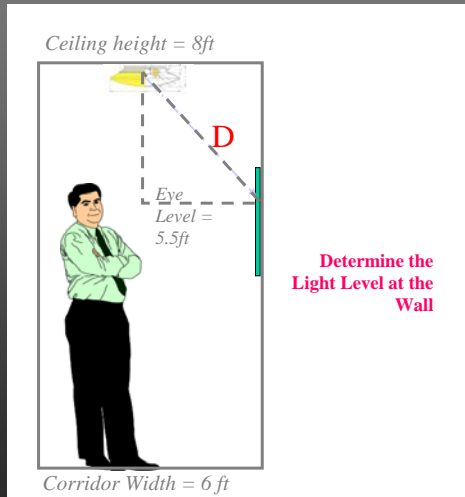


## Lighting Math

### Point-by-Point

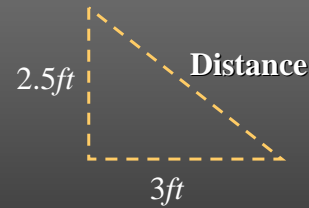
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



To solve for **D**, you can:

1. Scale the Drawing, or
2. Use Trigonometry



$$A^2 + B^2 = C^2$$

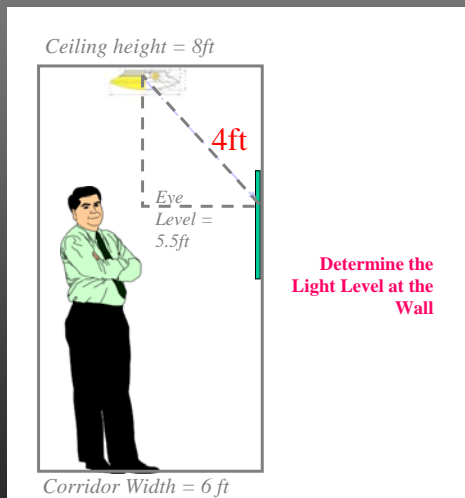
$$2.5^2 + 3^2 = C^2 \quad C = \sqrt{(6.25 + 9)}$$

$$6.25 + 9 = C^2 \quad C = 3.9 \text{ (approx 4ft)}$$

### Point-by-Point

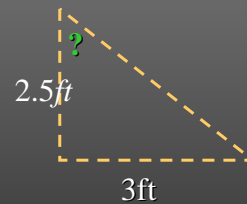
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



To solve for **Angle**, you can:

1. Scale the Drawing, or
2. Use Trigonometry



$$\tan(\text{Angle}) = \text{Opp} / \text{Adj}$$

$$\text{Angle} = \tan^{-1}(\text{Opp} / \text{Adj})$$

$$\text{Angle} = \tan^{-1}(3 / 2.5)$$

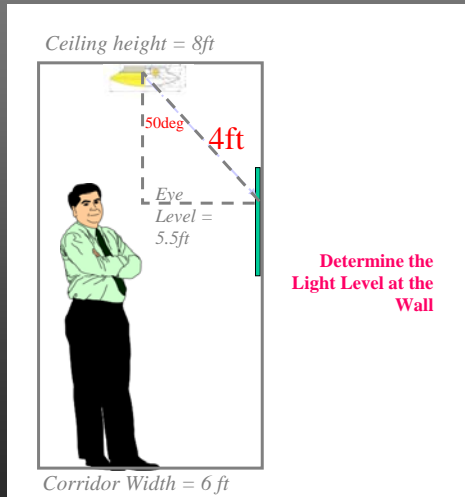
$$\text{Angle} = 50 \text{ degrees}$$

## Lighting Math

### Point-by-Point

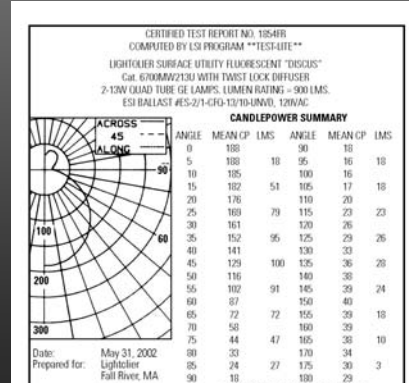
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



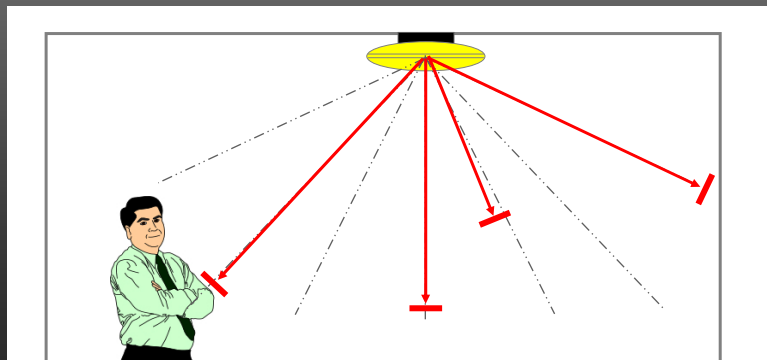
$$\text{FC} = \frac{\text{candelas}}{\text{ft}^2}$$

$$\text{FC} = \frac{\text{foot-candles}}{\text{ft}^2}$$



### Point-by-Point Factors

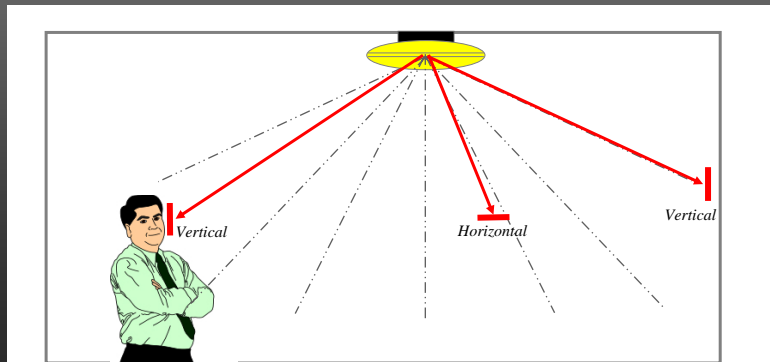
- Calculated Levels are Facing the Light Fixture
  - With the exception of directly below



## Lighting Math

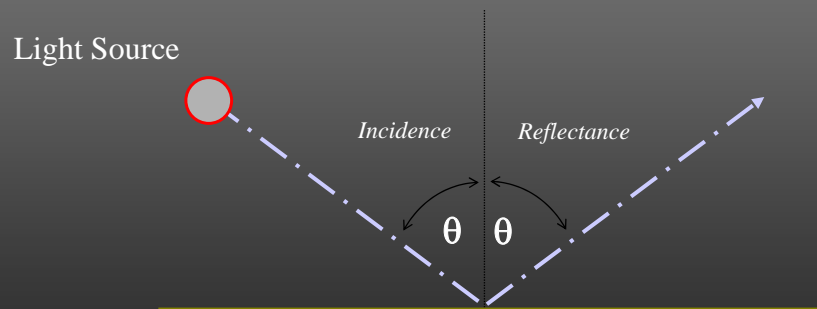
### Point-by-Point Factors

- You need to factor an adjustment if you want levels at other angles (IE Horizontal, Vertical Angles)
  - COSINE Adjusted!!



### COSINE Adjustments

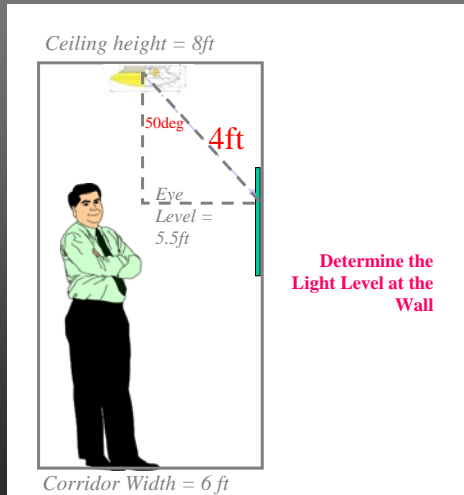
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2} \times \text{COS}(\text{Angle of Incidence})$$



## Lighting Math

## Point-by-Point... with COSINE Adjustment

- Ceiling Fixture Example



$$FC = CP/D^2 \times \cos(\text{angle})$$

## What is the Angle of Incidence?

$$FC = 7.25 \times \cos ( \_\_\_\_\_\_ \text{ deg} )$$

**FC** = \_\_\_\_ *foot-candles*

# Methods to Calculate Light

## Point-by-Point

- Direct Illumination from a Fixture or Lamp
  - You need....
    - Photometry
    - Distances from Fixture or Lamp

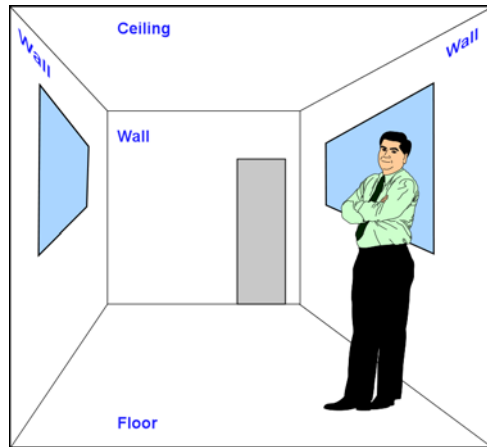
## Lumen Method

- Average Light Level in a Room from a Fixture
  - You need....
    - Photometry
    - Room Dimensions and Surface Reflectance's



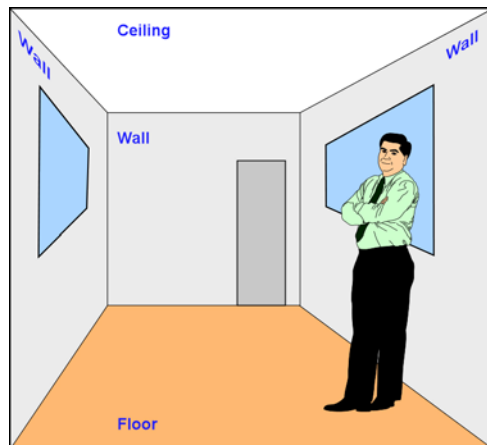
## Lighting Math

### Room Reflectance



- Room comprised of Walls, Ceiling, and Floor.
- Walls typically have Doors and Windows
- All surfaces have a reflectance value to bounce light.
- Light from Light Fixture bounces off of all surfaces.

### Room Reflectance



- Surfaces with less reflectance will bounce less light
- Typical Reflectance Values:
  - 75%-90% White, Off White, Grey, Light tints of Blue or Brown
  - 30%-60% Medium Green, Yellow, Brown, or Grey
  - 10%-20% Dark Grey, Medium Blue
  - 5%-10% Dark Blue, Brown, Dark Green, and many wood finishes

# Lighting Math

## Calculations using Lumens

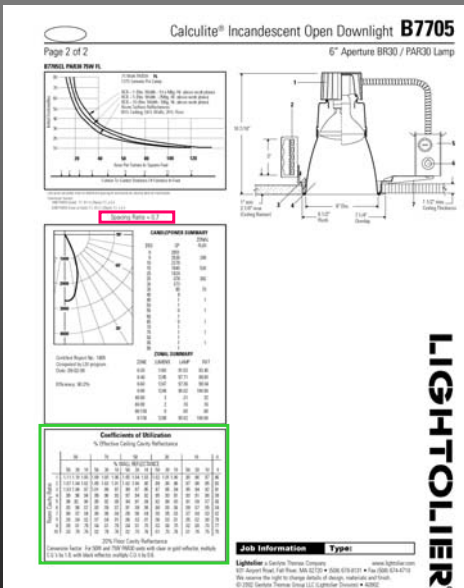
- Lumen Method Calculation

- Calculates the **Average Illumination** for a room.
- Takes into account the room surface reflectance's – but assumes the surfaces are diffuse (not shiny!).
- Assumes an empty room (without furniture).
- Can also be used to **determine the required Quantity of Fixtures** needed for a target light level.
- Does not determine light fixture layout or location – you must following mnfrs spacing criteria.

1. You need Room Dimensions and the Fixture Mounting Height.
2. You need to select a Light fixture
3. Determine the rooms Room Cavity Ratio (RCR).
4. Look-up the fixtures Coefficient of Utilization for the RCR.
5. Calculate!

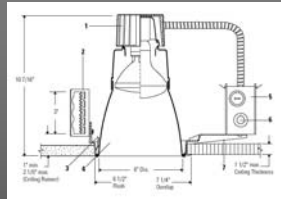
# Photometry Reports

- Plot of candlepower values
- Summary of candlepower values in different planes
- Fixture Efficiency
- Lumen Summary
- Luminance summary
- **Spacing Criteria (SC)** or Spacing/Mounting Height (S/MH) for uniformity
- **Coefficient of Utilization Table**
- **Guides**



## Lighting Math

### Coefficient of Utilization

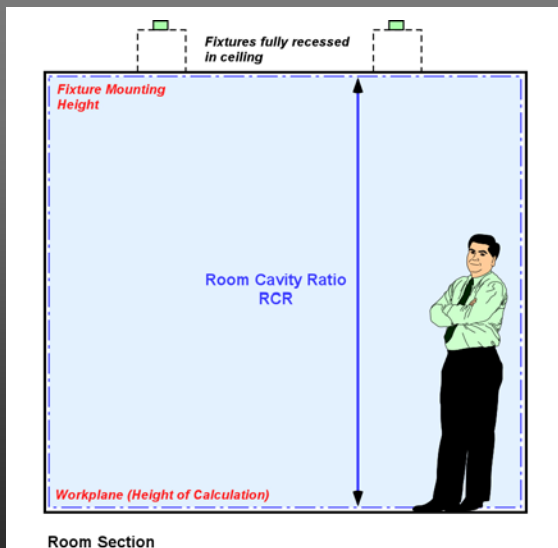


		Coefficients of Utilization									
		% Effective Ceiling Cavity Reflectance									
Room Cavity Ratio		% WALL REFLECTANCE									
		50	30	10	50	30	10	50	30	10	0
1	1.11	1.10	1.00	1.09	1.00	1.06	1.05	1.04	1.03	1.02	1.01
2	1.07	1.04	1.02	1.05	1.03	1.01	1.02	1.00	.98	.97	.96
3	1.03	1.00	.97	1.01	.99	.97	.99	.97	.95	.94	.93
4	.99	.96	.94	.99	.96	.93	.97	.94	.92	.91	.90
5	.96	.92	.90	.95	.92	.89	.94	.91	.89	.87	.86
6	.93	.90	.87	.93	.89	.87	.91	.88	.86	.85	.84
7	.90	.87	.84	.90	.86	.84	.88	.86	.84	.83	.82
8	.86	.84	.82	.87	.84	.81	.86	.83	.81	.80	.79
9	.85	.81	.79	.84	.81	.79	.84	.81	.79	.78	.77
10	.83	.79	.76	.82	.79	.76	.82	.79	.76	.75	.75

- Also known as **CU**
- Defines the percentage of light output that is expected from a fixture
- The value is determined by a CU table
- For commercial Reflectance of **80/50/20**, the actual CU value is this.

### Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L + W)}{\text{Room Area}}$$

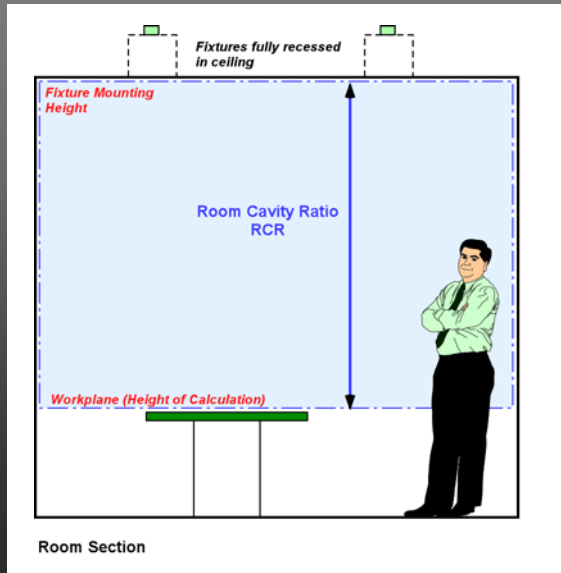


- The **RCR** can vary depending on the height you want to calculate...**as shown here with the calculation height at the floor.**

# Lighting Math

## Room Cavity Ratio

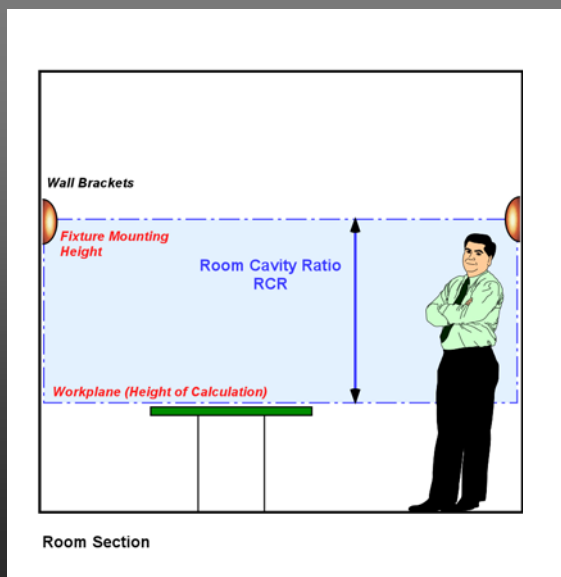
$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



- Room Cavity Ratio (aka **RCR**) is the volume between the **Fixture** and **Height of Calculation**
- Workplane height is typically 30-inches above the floor
- A room's RCR will always be between 1 and 10

## Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$

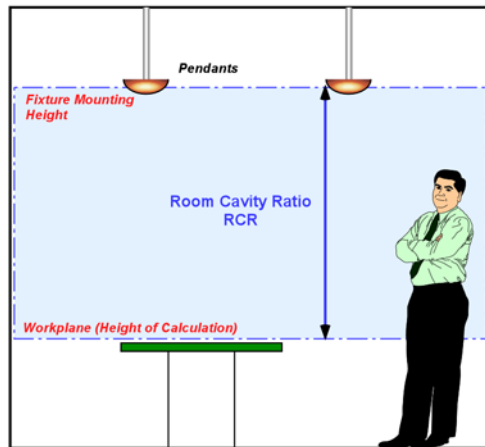


- The **RCR** can vary depending on the height of the fixture....**as shown here with Wall Brackets or Sconces.**

# Lighting Math

## Room Cavity Ratio

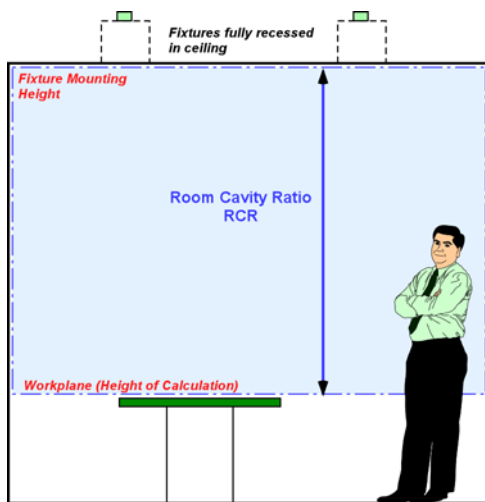
$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



- The **RCR** can vary depending on the height of the fixture....**as shown here with Pendants.**

## Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



Example:

Room Width: 12ft  
Room Length: 15ft  
Ceiling Height: 10ft

$$RCR = \frac{5 \times ( \quad ) \times ( \quad + \quad )}{( \quad \times \quad )}$$

RCR =

# Lighting Math

## Lumen Method Formula

To Calculate Foot-candle level:

$$FC = \frac{\text{Qty of Fixtures} \times \text{Number of Lamps per Fixture} \times \text{Lumens per Lamp} \times CU}{\text{Area of the Room}}$$

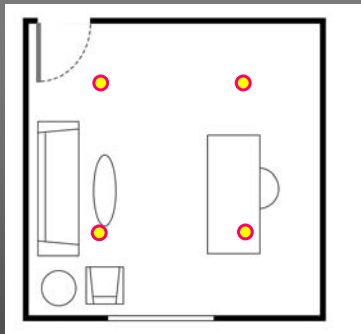
To Calculate number of Fixtures:

$$FC = \frac{\text{Total Lumens in the Room} \times CU}{\text{Area of the Room}}$$

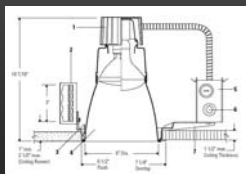
$$\text{Qty of Fixtures} = \frac{FC \times \text{Area of the Room}}{\text{Number of Lamps per Fixture} \times \text{Lumens per Lamp} \times CU}$$

$$\text{Qty of Fixtures} = \frac{FC \times \text{Area of the Room}}{\text{Total Lumens in the Room} \times CU}$$

## Lumen Method Example 1



What is the resulting Foot-candle Level at table height from four downlights?

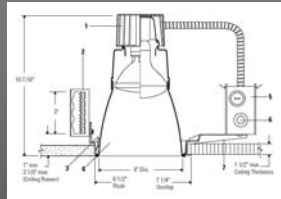


Example:  
Room Width: 12ft  
Room Length: 15ft  
Ceiling Height: 10ft

Lumen Method Calculation	
Project: _____	
Room/Area: _____	
Room Cavity Ratio:	
Room Width (W): _____	
Room Length (L): _____	
Fixture Mtg Height (MH): _____	
$RCR = \frac{5 \times (MH) \times (L + W)}{L \times W}$	
$RCR = \frac{5 \times ( ) \times ( ) + ( )}{ \times }$	
RCR = _____	
Irregular Room	
$RCR = \frac{2.5(MH) \times (Perimeter Length)}{Area}$	
Calculation:	
Fixture Description: _____	CU: _____
Lamp: _____	Lamps per Fixture: _____ Lumens per Lamp: _____
$FC = \frac{(\text{Qty of Fixtures}) \times (\text{Lumens per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}{L \times W}$	
$FC = \frac{( ) \times ( ) \times ( ) \times ( ) \times ( )}{( ) \times ( )}$	
FC = _____	
Qty of Fixtures = $\frac{FC \times L \times W}{(\text{Lumens per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}$	
$Qty \text{ of Fixtures} = \frac{( ) \times ( ) \times ( ) \times ( ) \times ( )}{( ) \times ( ) \times ( ) \times ( ) \times ( )}$	
Qty of Fixtures = _____	

## Lighting Math

### Coefficient of Utilization



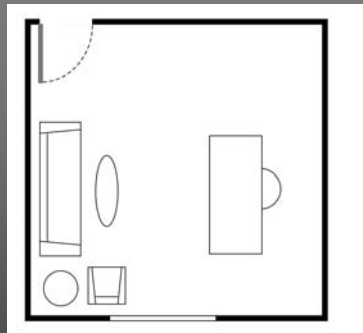
**Coefficients of Utilization**  
% Effective Ceiling Cavity Reflectance

Room Cavity Ratio	% WALL REFLECTANCE											
	50		70		50		30		10		0	
1	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04	1.03	1.02	1.01	1.00
2	1.07	1.04	1.02	1.01	1.01	1.00	0.99	0.98	0.97	0.96	0.95	0.94
3	1.03	1.00	0.97	0.95	0.93	0.91	0.89	0.87	0.85	0.84	0.82	0.81
4	0.99	0.96	0.94	0.92	0.90	0.88	0.86	0.84	0.82	0.81	0.79	0.78
5	0.96	0.93	0.91	0.89	0.87	0.85	0.83	0.81	0.79	0.78	0.76	0.75
6	0.93	0.90	0.87	0.85	0.83	0.81	0.79	0.77	0.75	0.74	0.72	0.71
7	0.90	0.87	0.84	0.82	0.80	0.78	0.76	0.74	0.72	0.71	0.69	0.68
8	0.87	0.84	0.82	0.80	0.78	0.76	0.74	0.72	0.70	0.69	0.67	0.66
9	0.85	0.81	0.79	0.77	0.75	0.73	0.71	0.69	0.67	0.66	0.64	0.63
10	0.83	0.79	0.76	0.74	0.72	0.70	0.68	0.66	0.64	0.63	0.61	0.60

20% Floor Cavity Reflectance  
Conversion Factor: For 50W and 75W PAR30 units with clear or gold reflector, multiply C.U.'s by 1.0; with black reflector, multiply C.U.'s by 0.6.

- Also known as **CU**
- Defines the percentage of light output that is expected from a fixture
- The value is determined by a CU table
- For our example:
- RCR \_\_\_\_\_
- the CU is \_\_\_\_\_
- For commercial Reflectance of **80/50/20**, the actual CU value is this.

### Lumen Method Example 2



How many fixtures do I need to achieve 30-foot-candles at table height?



**Lumen Method Calculation**

Project: \_\_\_\_\_

Room/Area: \_\_\_\_\_

Room Cavity Ratio:

Room Width (W): \_\_\_\_\_

Room Length (L): \_\_\_\_\_

Fixture Mtg Height (MH): \_\_\_\_\_

$RCR = \frac{5 \times (MH) \times (L + W)}{L \times W}$

$RCR = \frac{5 \times ( ) \times ( )}{ \times }$

RCR = \_\_\_\_\_

Irregular Room

$RCR = \frac{2.5 \times (MH) \times (Perimeter Length)}{Area}$

Calculation:

Fixture Description: \_\_\_\_\_ CU: \_\_\_\_\_

Lamp: \_\_\_\_\_ Lamps per Fixture: \_\_\_\_\_ Lumens per Lamp: \_\_\_\_\_

$FC = \frac{(Qty \text{ of Fixtures}) \times (Lumens \text{ per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}{L \times W}$

$FC = \frac{ \times \times \times \times \times }{ \times \times }$

FC = \_\_\_\_\_

$Qty \text{ of Fixtures} = \frac{FC \times L \times W}{(Lumens \text{ per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}$

$Qty \text{ of Fixtures} = \frac{ \times \times \times \times \times }{ \times \times \times \times \times }$

Qty of Fixtures = \_\_\_\_\_